

# Package ‘cata’

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**Type** Package

**Title** Analysis of Check-All-that-Apply (CATA) Data

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**Description** Functions for analyzing check-all-that-apply (CATA) data from consumer and sensory tests. Cochran's Q test, McNemar's test, and Penalty-Lift analysis provided, as described in for CATA data analysis by Meyners, Castura & Carr (2013) <[doi:10.1016/j.foodqual.2013.06.010](https://doi.org/10.1016/j.foodqual.2013.06.010)>. Cluster analysis can be performed using b-cluster analysis. The quality of cluster analysis solutions can be evaluated using various measures. The methods related to b-cluster analysis are described in a manuscript by Castura, Meyners, Varela & Naes (2022) <[doi:10.1016/j.foodqual.2022.104564](https://doi.org/10.1016/j.foodqual.2022.104564)>.

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**Index****17****barray***Convert 3d array of CATA data to 4d array of CATA differences***Description**

Converts a three-dimensional array (I assessors, J products, M attributes) to a four-dimensional array of product comparisons (I assessors, J(J-1)/2 product comparisons, two outcomes (of type b or c), M attributes)

**Usage**

```
barray(X, values = "bc", type.in = "binary", type.out = "binary")
```

**Arguments**

|          |   |
|----------|---|
| X        | three-dimensional array (I assessors, J products, M attributes) where values are 0 (not checked) or 1 (checked) |
| values   | "bc" (default) returns two outcomes: b and c; otherwise "abcd" returns four outcomes: a, b, c, d.               |
| type.in  | type of data submitted; default (binary) may be set to ordinal or scale.  |
| type.out | currently only binary is implemented  |

**Value**

A four-dimensional array of product comparisons having I assessors, J(J-1)/2 product comparisons, outcomes (see values parameter), M attributes

**References**

Castura, J.C., Meyners, M., Varela, P., & Næs, T. (2022). Clustering consumers based on product discrimination in check-all-that-apply (CATA) data. *Food Quality and Preference*, 104564. doi: [10.1016/j.foodqual.2022.104564](https://doi.org/10.1016/j.foodqual.2022.104564).

## Examples

```
data(bread)

# Get the 4d array of CATA differences for the first 10 consumers
b <- barray(bread$cata[1:10,,])
```

bcluster

*Wrapper function for b-cluster analysis*

## Description

By default, bcluster calls a function to perform b-cluster analysis by a non-hierarchical iterative ascent algorithm, then inspects results if there are multiple runs.

## Usage

```
bcluster(X, inspect = TRUE, inspect.plot = TRUE, algorithm = "n",
measure = "b", G = NULL, M = NULL, max.iter = 500, tol = exp(-32),
runs = 1, seed = 2021, verbose = FALSE)
```

## Arguments

|              |  |
|--------------|--|
| X            | three-way array with I assessors, J products, M attributes where CATA data have values 0 (not checked) and 1 (checked) |
| inspect      | default (TRUE) calls the <code>inspect</code> function to evaluate all solutions (when <code>runs&gt;1</code> )        |
| inspect.plot | default (TRUE) plots results from the <code>inspect</code> function  |
| algorithm    | default is n for non-hierarchical; h for hierarchical  |
| measure      | default is b for the b-measure; Q for Cochran's Q test   |
| G            | number of clusters (required for non-hierarchical algorithm)   |
| M            | initial cluster memberships  |
| max.iter     | maximum number of iteration allowed (default 500)  |
| tol          | non-hierarchical algorithm stops if variance over 5 iterations is less than tol (default: <code>exp(-32)</code> )      |
| runs         | number of runs (defaults to 1)   |
| seed         | for reproducibility (default is 2021)  |
| verbose      | maximum number of iterations   |

## Value

list with elements:

- `runs` : b-cluster analysis results from `bcluster.n` or `bcluster.h` (in a list if `runs>1`)
- `inspect` : result from `inspect` (the plot from this function is rendered if `inspect.plot` is TRUE)

## References

Castura, J.C., Meyners, M., Varela, P., & Næs, T. (2022). Clustering consumers based on product discrimination in check-all-that-apply (CATA) data. *Food Quality and Preference*, 104564. doi: [10.1016/j.foodqual.2022.104564](https://doi.org/10.1016/j.foodqual.2022.104564).

## Examples

```
data(bread)

# b-cluster analysis on the first 14 consumers and the first 6 attributes
(b1 <- bcluster(bread$cata[1:14,,1:6], G=2))
# identical to:
# (b2 <- bcluster.n(bread$cata[1:10,,1:6], G=2))
```

**bcluster.h**

*b-cluster analysis by hierarchical agglomerative strategy*

## Description

Perform b-clustering using the hierarchical agglomerative clustering strategy.

## Usage

```
bcluster.h(X, measure = "b", runs = 1, seed = 2021, verbose = FALSE)
```

## Arguments

|         |  |
|---------|--|
| X       | three-way array; the I, J, M array has I assessors, J products, M attributes where CATA data have values 0 (not checked) and 1 (checked) |
| measure | currently only b (the b-measure) is implemented  |
| runs    | number of runs (defaults to 1; use a higher number of runs for a real application)   |
| seed    | for reproducibility (default is 2021)  |
| verbose | maximum number of iterations   |

## Value

An object of class `hclust` from hierarchical b-cluster analysis results (a list of such objects if `runs>1`), where each `hclust` object has the structure described in `hclust` as well as the item `retainedB` (a vector indicating the retained sensory differentiation at each iteration (merger)).

## References

Castura, J.C., Meyners, M., Varela, P., & Næs, T. (2022). Clustering consumers based on product discrimination in check-all-that-apply (CATA) data. *Food Quality and Preference*, 104564. doi: [10.1016/j.foodqual.2022.104564](https://doi.org/10.1016/j.foodqual.2022.104564).

## Examples

```
data(bread)

# hierarchical b-cluster analysis on first 10 consumers and first 6 attributes
b <- bcluster.h(bread$cata[1:14,,1:6])

plot(as.dendrogram(b),
     main = "Hierarchical b-cluster analysis",
     sub = "10 bread consumers on 6 attributes")
```

**bcluster.n**

*b-cluster analysis by non-hierarchical iterative ascent clustering strategy*

## Description

Non-hierarchical b-cluster analysis transfers assessors iteratively to reach a local maximum in sensory differentiation retained.

## Usage

```
bcluster.n(X, G, M = NULL, measure = "b", max.iter = 500, runs = 1,
X.input = "data", tol = exp(-32), seed = 2021, verbose = FALSE)
```

## Arguments

|          |   |
|----------|---|
| X        | CATA data organized in a three-way array (assessors, products, attributes)                |
| G        | number of clusters (required for non-hierarchical algorithm)                              |
| M        | initial cluster memberships   |
| measure  | b (default) for the b-measure is implemented  |
| max.iter | maximum number of iteration allowed (default 500)   |
| runs     | number of runs (defaults to 1)  |
| X.input  | either "data" (default) or "bc" if X is obtained from the function <a href="#">barray</a> |
| tol      | algorithm stops if variance over 5 iterations is less than tol (default: $\exp(-32)$ )    |
| seed     | for reproducibility (default is 2021)   |
| verbose  | maximum number of iterations  |

## Value

An object of class `bclust.n` (or a list of such objects if `runs>1`), where each such object has the following components:

- `cluster` : vector of the final cluster memberships
- `totalB` : value of the total sensory differentiation in data set

- `retainedB` : value of sensory differentiation retained in b-cluster analysis solution
- `progression` : vector of sensory differentiation retained in each iteration
- `iter` : number of iterations completed
- `finished` : boolean indicates whether the algorithm converged before `max.iter`

## References

Castura, J.C., Meyners, M., Varela, P., & Næs, T. (2022). Clustering consumers based on product discrimination in check-all-that-apply (CATA) data. *Food Quality and Preference*, 104564. doi: [10.1016/j.foodqual.2022.104564](https://doi.org/10.1016/j.foodqual.2022.104564).

## Examples

```
data(bread)

# b-cluster analysis on the first 10 consumers and the first 6 attributes
(b <- bcluster.n(bread$cata[1:10, , 1:6], G=2))
```

`cochranQ`

*Cochran's Q test*

## Description

Calculate Cochran's Q test statistic. The null hypothesis that is assumed is that product proportions are all equal. The alternative hypothesis is that product proportions are not all equal.

## Usage

```
cochranQ(X, na.rm = TRUE, quiet = FALSE, digits = getOption("digits"))
```

## Arguments

|                     |   |
|---------------------|---|
| <code>X</code>      | matrix of I assessors (rows) and J products (columns) where values are 0 (not checked) or 1 (checked)             |
| <code>na.rm</code>  | should NA values be removed?  |
| <code>quiet</code>  | if FALSE (default) then it prints information related to the test; if TRUE it returns only the test statistic (Q) |
| <code>digits</code> | significant digits (to display)   |

## Value

Q test statistic

## References

Cochran, W. G. (1950). The comparison of percentages in matched samples. *Biometrika*, 37, 256-266.

Meyners, M., Castura, J.C., & Carr, B.T. (2013). Existing and new approaches for the analysis of CATA data. *Food Quality and Preference*, 30, 309-319, doi: [10.1016/j.foodqual.2013.06.010](https://doi.org/10.1016/j.foodqual.2013.06.010)

## See Also

[mcnemarQ](#)

## Examples

```
data(bread)

# Cochran's Q test on the first 40 consumers on the first attribute ("Fresh")
cochranQ(bread$cata[1:40,,1])
```

Consumer CATA data set: bread

*Consumer CATA data set: bread*

## Description

Raw results from CATA and Liking evaluations of six bread products samples by 161 consumers.

## Format

A list with 4 items:

- \$cata : check-all-that-apply (CATA) data (array, 161 consumers x 6 breads x 31 sensory attributes)
- \$liking : 9-point hedonic scale data (matrix, 161 consumers x 6 breads)
- \$ideal.cata : check-all-that-apply (CATA) data for ideal bread (matrix, 161 consumers x 31 sensory attributes)
- \$liking : 9-point hedonic scale data for ideal bread(vector, 161 consumers)

CATA data is coded 1 if the attribute is checked; otherwise it is coded 0

## References

Meyners, M., Castura, J.C., & Carr, B.T. (2013). Existing and new approaches for the analysis of CATA data. *Food Quality and Preference*, 30, 309-319, doi: [10.1016/j.foodqual.2013.06.010](https://doi.org/10.1016/j.foodqual.2013.06.010)

## Examples

```
data(bread)
head(bread$cata)
```

---

**evaluateClusterQuality***Evaluate Quality of Cluster Analysis Solution*

---

**Description**

Evaluate the quality of cluster analysis solutions using measures related to within-cluster product discrimination, between-cluster non-redundancy, overall diversity (coverage), average RV, sensory differentiation retained, and within-cluster homogeneity.

**Usage**

```
evaluateClusterQuality(X, M, alpha = .05, M.order = NULL,
quiet = FALSE, digits =getOption("digits"), ...)
```

**Arguments**

|         |   |
|---------|---|
| X       | three-way array; the I , J, M array has I assessors, J products, codeM attributes where CATA data have values 0 (not checked) and 1 (checked) |
| M       | cluster memberships   |
| alpha   | significance level to be used for two-tailed tests  |
| M.order | can be used to change the cluster numbers (e.g. to label cluster 1 as cluster 2 and vice versa); defaults to NULL                             |
| quiet   | if FALSE (default) then it prints information quality measures; if TRUE then returns results without printing                                 |
| digits  | significant digits (to display)   |
| ...     | other parameters for <a href="#">print.default</a> (if quiet = TRUE).   |

**Value**

A list containing cluster analysis quality measures:

- \$solution :
  - Pct.b = percentage of the total sensory differentiation retained in the solution
  - min(NR) = smallest observed between-cluster non-redundancy
  - Div\_G = overall diversity (coverage)
  - H\_G = overall homogeneity (weighted average of within-cluster homogeneity indices)
  - avRV = average RV coefficient for all between-cluster comparisons
- \$clusters :
  - ng = number of cluster members
  - bg = sensory differentiation retained in cluster
  - xbarg = average citation rate in cluster
  - Hg = homogeneity index within cluster (see [homogeneity](#))

- $D_g$  = within-cluster product discrimination
- \$nonredundancy.clusterpairs :
  - square data frame showing non-redundancy for each pair of clusters (low values indicate high redundancy)
- \$rv.clusterpairs :
  - square data frame with RV coefficient for each pair of clusters (high values indicate higher similarity in product configurations)

## References

Castura, J.C., Meyners, M., Varela, P., & Næs, T. (2022). Clustering consumers based on product discrimination in check-all-that-apply (CATA) data. *Food Quality and Preference*, 104564. doi: [10.1016/j.foodqual.2022.104564](https://doi.org/10.1016/j.foodqual.2022.104564).

## See Also

[homogeneity](#)

## Examples

```
data(bread)
evaluateClusterQuality(bread$cata[1:14,,1:6], M = rep(1:2, each = 7))
```

---

getb

*Calculate the b-measure*

---

## Description

Function to calculate the b-measure, which quantifies the sensory differentiation retained.

## Usage

```
getb(X.b, X.c)
```

## Arguments

- |     |  |
|-----|--|
| X.b | three-way ( $I, J(J-1)/2, M$ ) array with $I$ assessors, $J(J-1)/2$ product comparisons, $M$ CATA attributes, where values are counts of type b from the function <a href="#">barray</a> ) |
| X.c | array of same dimension as X.b, where values are counts of type b from the function <a href="#">barray</a> )   |

## Value

b-measure

## References

Castura, J.C., Meyners, M., Varela, P., & Næs, T. (2022). Clustering consumers based on product discrimination in check-all-that-apply (CATA) data. *Food Quality and Preference*, 104564. doi: [10.1016/j.foodqual.2022.104564](https://doi.org/10.1016/j.foodqual.2022.104564).

## Examples

```
data(bread)

bread.bc <- barray(bread$cata)
getb(bread.bc[1:10,,1,], bread.bc[1:10,,2,])
```

homogeneity

*Calculate within-cluster homogeneity*

## Description

Within a group of N consumers, the Homogeneity index lies between 1/N (no homogeneity) to 1 (perfect homogeneity).

## Usage

```
homogeneity(X)
```

## Arguments

X three-way array; the I, J, M array has I assessors, J products, codeM attributes where CATA data have values 0 (not checked) and 1 (checked)

## Value

homogeneity index

## References

Llobell, F., Cariou, V., Vigneau, E., Labenne, A., & Qannari, E. M. (2019). A new approach for the analysis of data and the clustering of subjects in a CATA experiment. *Food Quality and Preference*, 72, 31-39, doi: [10.1016/j.foodqual.2018.09.006](https://doi.org/10.1016/j.foodqual.2018.09.006)

## Examples

```
data(bread)

# homogeneity index for the first 7 consumers on the first 6 attributes
homogeneity(bread$cata[1:7,,1:6])
```

---

|         |   |
|---------|---|
| inspect | <i>Inspect/summarize many b-cluster analysis runs</i> |
|---------|---|

---

## Description

Inspect many runs of b-cluster analysis. Calculate sensory differentiation retained and recurrence rate.

## Usage

```
inspect(X, G = 2, bestB = NULL, bestM = NULL, inspect.plot = TRUE)
```

## Arguments

|              |  |
|--------------|--|
| X            | three-way array; the I, J, M array has I assessors, J products, codeM attributes where CATA data have values 0 (not checked) and 1 (checked)           |
| G            | number of clusters (required for non-hierarchical algorithm)   |
| bestB        | total sensory differentiation retained in the best solution. If not provided, then bestB is determined from best solution in the runs provided (in X). |
| bestM        | cluster memberships for best solution. If not provided, then the best solution is determined from the runs provided (in X).                            |
| inspect.plot | default (TRUE) plots results from the <code>inspect</code> function  |

## Value

A data frame with unique solutions in rows and the following columns:

- B : Sensory differentiation retained
- pctB : Percentage of the total sensory differentiation retained
- B.prop : Proportion of sensory differentiation retained compared to best solution
- raw.agree : raw agreement with best solution
- count : number of runs for which this solution was observed
- c.1, c.2, ... : remaining columns gives index of the cluster to which the consumers (columns) are allocated

## References

Castura, J.C., Meyners, M., Varela, P., & Næs, T. (2022). Clustering consumers based on product discrimination in check-all-that-apply (CATA) data. *Food Quality and Preference*, 104564. doi: [10.1016/j.foodqual.2022.104564](https://doi.org/10.1016/j.foodqual.2022.104564).

## Examples

```
data(bread)
res <- bcluster.n(bread$cata[1:10, , 1:8], G = 2, runs = 5)
inspect(res)
```

**mcnemarQ***McNemar's test***Description**

Pairwise tests are conducted using the two-tailed binomial test. These tests can be conducted after Cochran's Q test.

**Usage**

```
mcnemarQ(X, na.rm = TRUE, quiet = FALSE, digits = getOption("digits"))
```

**Arguments**

|        |   |
|--------|---|
| X      | matrix of I assessors (rows) and J products (columns) where values are 0 (not checked) or 1 (checked)             |
| na.rm  | should NA values be removed?  |
| quiet  | if FALSE (default) then it prints information related to the test; if TRUE it returns only the test statistic (Q) |
| digits | significant digits (to display)   |

**Value**

Test results for all McNemar pairwise tests conducted via the binomial test

**References**

- Cochran, W. G. (1950). The comparison of percentages in matched samples. *Biometrika*, 37, 256-266.
- McNemar, Q. (1947). Note on the sampling error of the difference between correlated proportions or percentages. *Psychometrika*, 12(2), 153-157.
- Meynens, M., Castura, J.C., & Carr, B.T. (2013). Existing and new approaches for the analysis of CATA data. *Food Quality and Preference*, 30, 309-319, doi: [10.1016/j.foodqual.2013.06.010](https://doi.org/10.1016/j.foodqual.2013.06.010)

**See Also**

[cochranQ](#)

**Examples**

```
data(bread)

# McNemar's exact pairwise test for all product pairs
# on the first 40 consumers and the first attribute ("Fresh")
mcnemarQ(bread$cata[1:40,,1])
```

---

**pLift***Penalty-Lift Analysis*

---

**Description**

Penalty-Lift analysis for CATA variables, which is the difference between the average hedonic response when CATA attribute is checked vs. the average hedonic response when CATA attribute is not checked.

**Usage**

```
pLift(X, Y)
```

**Arguments**

- X      either a matrix of CATA data with I consumers (rows) and J products (columns)  
or an array of CATA data with I consumers, J products, and M attributes.
- Y      matrix of hedonic data with I consumers (rows) and J products (columns)

**Value**

Penalty lift for the attribute if X is a matrix; otherwise, penalty-lift for each attribute if X is a 3d array.

**References**

Meyners, M., Castura, J.C., & Carr, B.T. (2013). Existing and new approaches for the analysis of CATA data. *Food Quality and Preference*, 30, 309-319, doi: [10.1016/j.foodqual.2013.06.010](https://doi.org/10.1016/j.foodqual.2013.06.010)

**Examples**

```
data(bread)

# penalty lift, based only on the first 20 consumers

# for the first attribute ("Fresh")
pLift(bread$cata[1:20,,1], bread$liking[1:20, ])

# for the first 3 attributes
pLift(bread$cata[1:20,,1:3], bread$liking[1:20, ])
```

|                      |                                 |
|----------------------|---------------------------------|
| <code>rv.coef</code> | <i>Calculate RV Coefficient</i> |
|----------------------|---------------------------------|

### Description

Calculate RV coefficient

### Usage

```
rv.coef(X, Y, method = 1)
```

### Arguments

|        |  |
|--------|--|
| X      | input matrix (same dimensions as Y)              |
| Y      | input matrix (same dimensions as X)              |
| method | 1 (default) and 2 give identical RV coefficients |

### Value

RV coefficient

### References

Robert, P., & Escoufier, Y. (1976). A unifying tool for linear multivariate statistical methods: the RV-coefficient. *Journal of the Royal Statistical Society: Series C (Applied Statistics)*, 25, 257-265.

### Examples

```
# Generate some data
set.seed(123)
X <- matrix(rnorm(8), nrow = 4)
Y <- matrix(rnorm(8), nrow = 4)

# get the RV coefficient
rv.coef(X, Y)
```

|                     |                                |
|---------------------|--------------------------------|
| <code>salton</code> | <i>Salton's cosine measure</i> |
|---------------------|--------------------------------|

### Description

Calculate Salton's cosine measure

### Usage

```
salton(X, Y)
```

**Arguments**

|   |                                     |
|---|-------------------------------------|
| X | input matrix (same dimensions as Y) |
| Y | input matrix (same dimensions as X) |

**Value**

Salton's cosine measure

**References**

Salton, G., & McGill, M.J. (1983). *Introduction to Modern Information Retrieval*. Toronto: McGraw-Hill.

**Examples**

```
# Generate some data
set.seed(123)
X <- matrix(rnorm(8), nrow = 4)
Y <- matrix(rnorm(8), nrow = 4)

# get Salton's cosine measure
salton(X, Y)
```

toMatrix

*Converts 3d array of CATA data to a tall 2d matrix format*

**Description**

Converts a three-dimensional array (I assessors, J products, M attributes) to a two-dimensional matrix with (I assessors, J products) rows and (M attributes) columns, optionally preceded by two columns of row headers.

**Usage**

```
toMatrix(X, header.rows = TRUE)
```

**Arguments**

|             |   |
|-------------|---|
| X           | three-dimensional array (I assessors, J products, M attributes) where values are 0 (not checked) or 1 (checked) |
| header.rows | TRUE (default) includes row headers; set to FALSE to exclude these headers                                      |

**Value**

A matrix with I assessors \* J products in rows and M attributes in columns (preceded by 2 columns of headers if header.rows = TRUE)

## Examples

```
data(bread)

# convert CATA results from the first 10 consumers and the first 4 attributes
# to a tall matrix
toMatrix(bread$cata[1:10,,1:4])
```

**toWideMatrix**

*Converts 3d array of CATA data to a wide 2d matrix format*

## Description

Converts a three-dimensional array (I assessors, J products, M attributes) to a two-dimensional matrix (J products, (I assessors, M attributes))

## Usage

```
toWideMatrix(X)
```

## Arguments

|   |   |
|---|---|
| X | three-dimensional array (I assessors, J products, M attributes) where values are 0 (not checked) or 1 (checked) |
|---|---|

## Value

A matrix with J products in rows and I assessors \* M attributes in columns

## Examples

```
data(bread)

# convert CATA results from the first 10 consumers and the first 4 attributes
# to a wide matrix
toWideMatrix(bread$cata[1:10,,1:4])
```

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